
EXACT ALLOCATIVE AND TECHNICAL INEFFICIENCY USING THE NORMALIZED QUADRATIC COST FUNCTION

Juan José Díaz Hernández (*), Eduardo Martínez Budría (*), Sergio R. Jara-Díaz (**)
(*) Instituto Universitario de Desarrollo Regional y Departamento de Análisis Económico.
Universidad de La Laguna. España. Camino de La Hornera s/n, 38001 La Laguna, S/C de

Tenerife. España

(**) Departamento de Ingeniería Civil, Universidad de Chile. Chile
jjodiaz@ull.es, embudria@ull.es, jaradiaz@ing.uchile.cl

ABSTRACT

In this paper we have built a theoretical model using a normalized quadratic cost system to obtain expressions for actual input demand and cost as functions of three components: frontier, allocative and technical inefficiency. We have used the shadow prices approach in the line of exact decomposition that allows solving Greene's problem. Using the normalized quadratic cost system has permitted to isolate not only allocative inefficiency but also the technical one, as simple functions of both parameters and variables. The model allows obtaining individual and time varying technical and allocative inefficiency measures when a panel data is available. This model has been applied to cargo handling in Spanish ports.

1. INTRODUCTION

The estimation of efficiency through the stochastic cost frontier approach does not permit the correct decomposition of inefficiency into its technical and allocative components. This occurs because the error component that captures the allocative inefficiency and that which represents total inefficiency are not statistically independent and, therefore, parameter estimates are inconsistent (Greene, 1980b). This is known in the literature as "Greene's problem" (Bauer, 1990b), and induces distortions on the technical characteristics and on the identification of the productivity components when these are analysed through stochastic costs frontier models.

The attempts to solve Greene's problem based on trans-logarithmic stochastic frontiers, specify the relations between the error components of the cost function and the share equations. This approach to Greene's problem has two disadvantages. First of all, the impact of inefficiency on shares and costs cannot depend on the levels of outputs and/or on the prices of inputs. Secondly, errors in the chosen specification bring a bias into the estimations obtained.

The shadow price approach is an alternative procedure where inefficiency is captured through a set of parameters that are jointly estimated with those characterizing technology. On one hand, input oriented technical inefficiency has been modelled by Atkinson and Cornwell (1994a) by scaling the input vector in the cost function through a parameter that is the inverse of the input oriented technical efficiency index proposed by Farrell (1957). Besides, they modelled the output oriented technical inefficiency using a parameter that indicates how the observed outputs are deviated from maximum output levels. On the other hand, the strategy followed for the analysis of allocative inefficiency has been the definition of unobserved input prices, named shadow prices, for which the observed input combination would be optimal. Along this line, Atkinson and Cornwell (1994b) estimated cost inefficiency in a panel data context using a translog cost system. Following the approach designed to analyse allocative inefficiency, Kumbhakar (1997) proposed a model that incorporates both technical and allocative inefficiency in a translog cost system using input oriented technical inefficiency. In this way, he deduced the exact relation between allocative inefficiency, and its impact on costs and the share equations of each input, in a theoretically consistent fashion for a trans-logarithmic specification. Greene's problem is solved theoretically using the shadow input prices approach. The empirical applications of this model are scarce, and they all use the translog-based equations system. Among these, Maietta (2000) introduces technical inefficiency as fixed individual effects and allocative inefficiency as parameters that are functions of time trend and individual dummy variables. Recently, Kumbhakar and Tsionas (2005) have estimated this model using the Bayesian approach in a translog cost system.

The main objective of this paper is to build a model to show, in the line of exact decomposition, the three components of input quantities and actual cost: frontier, technical inefficiency effect, and allocative inefficiency impact, for the normalized quadratic cost function. For this proposal we use the shadow price approach.

This model presents three novelties regarding previous work. First, we have modelled allocative and technical inefficiency exactly for a normalized quadratic cost function. This function presents advantages regarding the usual translogarithmic specification. Thus, deviations of optimal input demands and cost are simple functions of allocative inefficiency. Besides, this specification

belongs to the family of flexible functions and has the advantage of being defined for zero output levels, a relevant property when dealing with multioutput activities because observations usually include zeroes for some firms' products during some periods, and because the analysis of economies of scope requires the valuation of outputs in zero. The second novelty is to model separately both allocative and technical inefficiency as function of the model parameters, input prices and outputs. This exercise is done both for inputs demands and cost function. The third is a difference regarding Kumbhakar and Tsionas (2004), as we propose a non-linear least squares econometric procedure. As we use panel data for the application of the model, we will see that the exact measures for each type of inefficiency can be obtained for each firm and period considered.

To examine empirically the properties of the theoretical model, it is applied to the analysis of cargo handling operations in Spanish ports during the nineties. This is a particularly attractive exercise as this activity, a key component in the logistic chain, has been described as traditionally inefficient in the specialized literature, as a consequence of the control exercised by local labour monopolies in practically all ports around the world.

The rest of the paper is structured as follows. Section 2 describes the procedure based on the shadow prices approach under a quadratic specification in order to model the allocative inefficiency first, and then extended to total inefficiency. In Section 3 the application is presented. Finally, in Section 4 the main conclusions of this work are presented.

2. THE MODEL

2.1 Allocative Inefficiency Through The Shadow Cost Function

This section brings in the effect of allocative inefficiency assuming that the agent behaves in a technically efficient manner, denoted by the *te* sub index.

Let $X_{te} = (X_{1,te}, \dots, X_{m,te})$ be a vector of m inputs and W the corresponding price vector, with W^S as the shadow price vector for which the combination of actual inputs is allocatively efficient. Therefore, the marginal productivity ratio is equal to the shadow prices ratio for each pair of inputs, i.e.:

$$\frac{f_i(X_{te})}{f_k(X_{te})} = \frac{W_i^S}{W_k^S} \quad (1)$$

where $f_i(X_{te})$ is the marginal product of input i . Toda (1976), Atkinson and Halvorsen (1984, 1990) and Eakin (1993) suggest that relative shadow prices be defined as a multiplicative parametric correction of relative actual prices, that is:

$$\frac{f_i(X_{te})}{f_k(X_{te})} = \frac{W_i}{W_k} \varepsilon_i \quad (2)$$

where ε_i represents a specific parameter that indicates how the relative actual prices between input i and k deviates from the relative shadow price ratio (obviously $\varepsilon_i > 0$, $i \neq k$).

If $\varepsilon_i = 1$, then the relative shadow price is the same as its relative actual price and, therefore, the chosen combination of production factors is allocatively efficient. On the other hand, if $\varepsilon_i < 1$, then

the relative shadow price is lower than its relative actual price, and then the actual demand of input i exceeds the efficient quantity. On the contrary, if $\varepsilon_i > 1$, the producer has chosen a quantity that is below the efficient quantity.

The parameters that link market prices with their corresponding shadow prices are specified accounting for variations in time that also imposes non-negativity. As pointed out by Kumbhakar (1992), cost reductions in time can be caused both by technical change and by variations in allocative efficiency. This procedure avoids possible bias in the measure of technical change. Therefore

$$\varepsilon_{it} = (1 + \eta_i + \eta_{it})^2 = 1 + \Omega_{it}; i \neq k \quad (3)$$

where Ω_{it} is the deviation of the relative price of input i from the relative shadow price at period t . By definition, $-1 < \Omega_{it} < \infty$. In what follows, the time sub-index will be suppressed to simplify notation.

With this reformulation of the conditions for minimising costs in terms of shadow prices, the technically efficient combination of inputs, X_{te} , is the solution to a problem of cost minimisation that considers shadow prices (W^S), which differs from the solution chosen by the producer, where the prices that explain his decision are market prices (W). Formally, the shadow cost function corresponds to

$$C_{te}(W^S, Q) = \min_x [W^S X_{te} / F(X_{te}, Q) = 0] = \sum_{i=1}^m W_i^S X_{i,te}(W^S, Q) \quad (4)$$

where $C_{te}(W^S, Q)$ is the minimum cost to obtain the output vector $Q = (Q_1, \dots, Q_n)$ when the price vector is W^S , and $F(X_{te}, Q) = 0$ represents an optimum use of technology.

Let us define C_{te} as the actual expenditure under technical efficiency, which is the sum of the actual expenses on each technically efficient input. Using the definition of shadow prices given by (2) and (3), we obtain:

$$C_{te} = \sum_{i=1}^m W_i X_{i,te}(W^S, Q, t) = C_{te}(W^S, Q, t) - \sum_{i \neq k} \Omega_i W_i X_{i,te}(W^S, Q, t) \quad (5)$$

Expression (5) decomposes C_{te} into two terms. The first is the shadow cost function $C_{te}(W^S, Q, t)$ that indicates the minimum cost of producing the vector of outputs (Q), given the input shadow price vector (W^S). The second term represents the difference between C_{te} and the minimum cost assessed with shadow prices. This second component will be zero only if there is allocative efficiency.

To continue with the analysis, we have to adopt a concrete functional form that, in our case, is the normalized quadratic cost function (NQCF). Let the NQCF evaluated in W^S be

$$\begin{aligned} c_{te}(w^S, Q, t) = & \alpha_0 + \sum_{i \neq k} \alpha_i w_i^S + \sum_{k=1}^n \alpha_k Q_k + \frac{1}{2} \sum_{i \neq k} \sum_{j \neq k} \alpha_{ij} w_i^S w_j^S + \frac{1}{2} \sum_{r=1}^n \sum_{l=1}^n \alpha_{rl} Q_r Q_l + \\ & + \sum_{i \neq k} \sum_{r=1}^n \alpha_{ir} w_i^S Q_r + \sum_{i \neq k} \alpha_{ii} w_i^S t + \sum_{r=1}^n \alpha_{rr} Q_r t + \alpha_t t + \alpha_{tt} t^2 \end{aligned} \quad (6)$$

where $c_{te}(w^S, Q, t) = C_{te}(w^S, Q, t) / W_k^S$; $w^S = (W_1^S / W_k^S, \dots, W_m^S / W_k^S)$ and $W_k^S = W_K$

The price of input k has been used both to build the relative prices and to normalize the cost function to impose homogeneity of degree one. Also, we have added a time trend as a *proxy* variable representing technical change that interacts with output levels and the prices of inputs to account for possible biases.

We have to remember that the shadow price approach is based on the equality between the quantity of input i under technical efficiency and the efficient allocative demand for the input using shadow prices. This permits the application of Shephard's lemma to the shadow cost function defined in (6), i.e.

$$X_{i,te}(w^s, Q, t) = \frac{\partial c_{te}(w^s, Q, t)}{\partial w_i^s} = \alpha_i + \frac{1}{2} \sum_{j \neq k} \alpha_{ij} (1 + \Omega_j) w_j + \sum_{r=1}^n \alpha_{ir} Q_r + \alpha_{it} t \quad (7)$$

where w_j is the normalized actual price of input j .

Expression (7) can be decomposed into two terms,

$$X_{i,te}(w^s, Q, t) = X_i^*(w, Q, t) + X_i^{al}(w, \Omega) \quad (8)$$

The first component of (8) indicates the optimum level of input i , given the actual prices, i.e.

$$X_i^*(w, Q, t) = \alpha_i + \frac{1}{2} \sum_{j \neq k} \alpha_{ij} w_j + \sum_{r=1}^n \alpha_{ir} Q_r + \alpha_{it} t \quad (9)$$

The second component of (8) represents the impact of the allocative inefficiency on the demand for input i , that is

$$X_i^{al}(w, \Omega) = \frac{1}{2} \sum_{j \neq k} \Omega_j \alpha_{ij} w_j \quad (10)$$

Expression (10) shows the effect of allocative inefficiency on input demand i in a theoretically exact fashion. The effect is expressed as a function of the observed input prices, the parameters that determine the relationship between inputs (complements or substitutes) and the pattern of allocative inefficiency. The sign of (10) indicates whether allocative inefficiency leads to an excessive use or a saving of input i in comparison with efficient levels.

The decomposition of the actual technically efficient expenditure in equation (5) has been expressed in terms of shadow prices that are unknown to the researcher. Nonetheless, as shadow prices can be expressed as a parametric correction of prices, we can transform expression (5) in terms of actual input prices. For that, introducing (3) into (2), and using (6), we obtain the following expression for the normalized version of (5)

$$\begin{aligned} c_{te} = c_{te}(w^s, Q, t) - \sum_{i \neq k} \Omega_i w_i X_{i,te}(w^s, Q, t) &= \alpha_0 + \sum_{i \neq k} \alpha_i (1 + \Omega_i) w_i + \sum_{r=1}^n \alpha_r Q_r + \\ &+ \frac{1}{2} \sum_{i \neq k} \sum_{j \neq k} \alpha_{ij} (1 + \Omega_i) (1 + \Omega_j) w_i w_j + \frac{1}{2} \sum_{r=1}^n \sum_{l=1}^n \alpha_{rl} Q_r Q_l + \sum_{i \neq k} \sum_{r=1}^n \alpha_{ir} (1 + \Omega_i) w_i Q_r + \\ &+ \sum_{i \neq k} \alpha_{it} (1 + \Omega_i) w_i t + \sum_{r=1}^n \alpha_{rt} Q_r t + \alpha_{tt} t^2 - \sum_{i \neq k} \Omega_i w_i X_{i,te}(w^s, Q, t) \end{aligned} \quad (11)$$

This expression can be decomposed as

$$c_{te} = c^*(w, Q, t) + c^{al}(w, Q, t, X) \quad (12)$$

where the cost frontier, depending on actual input prices, is

$$c^*(w, Q, t) = \alpha_0 + \sum_{i \neq k} \alpha_i w_i + \sum_{r=1}^n \alpha_r Q_r + \frac{1}{2} \sum_{i \neq k} \sum_{j \neq k} \alpha_{ij} w_i w_j + \quad (13)$$

$$\frac{1}{2} \sum_{r=1}^n \sum_{l=1}^n \alpha_{rl} Q_r Q_l + \sum_{i \neq k} \sum_{r=1}^n \alpha_{ir} w_i Q_r + \sum_{i \neq k} \alpha_{it} w_i t + \sum_{r=1}^n \alpha_{rt} Q_r t + \alpha_t t + \alpha_{tt} t^2$$

while the impact of allocative inefficiency on cost, c^{al} , is:

$$c^{al} = \sum_{i \neq k} \alpha_i \Omega_i w_i + \sum_{i \neq k} \sum_{j \neq k} \alpha_{ij} \Omega_j w_i w_j + \frac{1}{2} \sum_{i \neq k} \sum_{j \neq k} \alpha_{ij} \Omega_i \Omega_j w_i w_j + \quad (14)$$

$$\sum_{i \neq k} \sum_{r=1}^n \alpha_{ir} \Omega_i w_i Q_r + \sum_{i \neq k} \alpha_{it} \Omega_i w_i t - \sum_{i \neq k} \Omega_i w_i X_{i,te}(w^S, Q, t)$$

Introducing in (14) the expression for $X_{i,te}$ obtained in (7) we get

$$c^{al}(w, \Omega) = \frac{1}{2} \sum_{j \neq k} \sum_{i \neq k} \alpha_{ij} \Omega_i w_i w_j = \sum_{j \neq k} w_j X_{j,te}^{al} \quad (15)$$

The first equality shows the impact of allocative inefficiency on costs. The second shows that it could have been obtained from input demands, $X_{j,te}^{al}$. In (15) we show the exact, and consistent with economic theory, expression of allocative inefficiency cost.

2.2 Modelling technical inefficiency

Now we will incorporate Farrell's (1957) technical inefficiency measure, which is input oriented. Let ϕ be the parameter that measures the proportional deviation of actual input used X_i^a from the technically efficient input values, i.e.

$$X_i^a = \phi X_{i,te}(w^S, Q, t); i = 1, \dots, m, \quad (16)$$

where $\phi \geq 1$ and $\phi = 1$ means technically efficient input usage.

Introducing (8) in (16), adding and subtracting $X_i^*(w, Q, t) + X_i^{al}$, we get

$$X_i^a = X_i^*(w, Q, t) + X_i^{al}(w, \Omega) + (\phi - 1) [X_i^*(w, Q, t) + X_i^{al}(w, \Omega)] \quad (17)$$

where the first term is the optimal demand for input i , obtained as in (9), the second is the impact of the allocative inefficiency on demand of input i obtained in (10), and the last term is the effect of technical inefficiency on factor i , X_i^{tech} . This latter can be written taking into account (9) and (10), as

$$X_i^{tech} = (\phi - 1) \left[\alpha_i + \frac{1}{2} \sum_{j \neq k} \alpha_{ij} (1 + \Omega_j) w_j + \frac{1}{2} \sum_{r=1}^n \alpha_{ir} Q_r + \alpha_{it} t \right] \quad (18)$$

Expression (18) links the impact of technical inefficiency on input demands with observed input prices and output levels, and with the parameters representing allocative and technical inefficiency, Ω and ϕ respectively.

In the same way, observed cost c^a can be expressed as:

$$c^a = \phi c_{te} \quad (19)$$

which makes it explicit that actual costs are directly proportional to the measure of technical inefficiency. Let us substitute the value of c_{te} from (12) into (19), adding and subtracting $c^*(w, Q, t) + c^{al}(w, \Omega)$. This yields

$$c^a = \phi \left(c^*(w, Q, t) + c^{al}(w, \Omega) \right) = c^*(w, Q, t) + c^{al}(w, \Omega) + (\phi - 1) \left[c^*(w, Q, t) + c^{al}(w, \Omega) \right] \quad (20)$$

The first component in expression (20) represents the cost frontier obtained in (13), the second is allocative inefficiency cost obtained in (15) and the last is technical inefficiency cost. This technical inefficiency cost, c^{tech} , can be expressed using equations (13) and (15)

$$c^{tech} = (\phi - 1) \left[\alpha_0 + \sum_{i \neq k} \alpha_i w_i + \sum_{r=1}^n \alpha_r Q_r + \frac{1}{2} \sum_{r=1}^n \sum_{l=1}^n \alpha_{rl} Q_r Q_l + \sum_{i \neq k} \sum_{r=1}^n \alpha_{ir} w_i Q_r + \sum_{i \neq k} \alpha_{it} w_i t + \sum_{r=1}^n \alpha_{rt} Q_r t + \alpha_{tt} t^2 + \frac{1}{2} \sum_{i \neq k} \sum_{j \neq k} \alpha_{ij} (1 + \Omega_i) w_i w_j \right] \quad (21)$$

From (13), (15) and (21) we obtain that input oriented Farrell's Indices can be calculated for each observation where CE is the Cost Efficiency Index defined in the following expression

$$0 \leq CE = \frac{C^*(W, Q, t)}{C^a} \leq 1 \quad (22)$$

TE is Technical Efficiency Index

$$TE = \frac{C_{te}(W^S, Q, t)}{C^a} \quad (23)$$

And AE is the Allocative Efficiency Index.

$$AE = \frac{C^*(W, Q, t)}{C_{te}} \quad (24)$$

Note, finally, that Farrell's index in equation (22) happens to be

$$CE = TE \times AE \quad (25)$$

3. AN APPLICATION TO CARGO HANDLING IN SPANISH PORTS

3.1 The Spanish cargo handling sector

Cargo handling involves all the movements of freight from arrival to the port to its location within the ship and vice versa, including loading and unloading, transshipment, reception and dispatch. Accordingly, it is the most important activity within a port. Different types of cranes, specialized labour and different types of vehicles are the most relevant production factors. Cargo handling has been usually a regulated activity and the need for specialized labour has generated groups of workers with monopolistic characteristics: the stevedores. In the Spanish case, it is felt

that until the eighties the law stimulated a disproportionate increase of workers, wages unrelated to productivity, and bad practices regarding the organization of work, like oversized teams and restricted schedules, causing low labour productivity and large prices for port services, diminishing Spanish ports competitiveness.

The reform that begun in the eighties aimed at more flexibility in the design of work teams and in the schedules, abandoning centralized regulation (state level) and permitting each firm to decide on team size and configuration within predetermined safety levels. Work periods can be increased to fulfil demand requirements, including night and weekend shifts. Wages and contracts are port specific collective agreements. As a result, the payroll has diminished and the design of work teams is now decentralized. Nevertheless, the opening of the activity to other firms, something which would lead to more competitive prices, has been non existent; and, in any case, in a subsidiary way and with the same wage level as if the work was done by workers of the SEED (Sociedades Estatales de Estiba y Desestiba). Given these characteristics, we believe it is an adequate sector to test the model developed in section 2.

3.2 Data

Cargo handling activities involve essentially two factors: labour and cranes. Data sources are the State Annual Reports on Ports, the Annual Report of each port and a questionnaire that we had drawn up and presented to the SEED. The data from the Annual Reports of the Ports of the State have been used to get the quantities of cargo moved by each port and year included in the sample. The outputs analysed in this study were defined according to how the merchandise is handled, which, in turn, will determine what kind of operation is needed to load or unload it. Thus, we can distinguish between general container cargo (*MGC*), non-containerised general cargo (*MGNC*) and solid bulk cargoes that are handled without special facilities (*GSSI*). The Annual Reports of each port and the information received from crane operators in ports have given us the hours worked by cranes and have permitted the calculation of total expenses on this item. The other data source, namely the questionnaire sent to all SEED, gave us important information on the labour factor, basically concerned with labour expenditure and hours worked by stevedores. To build input price indicators, we have the total expenditure on each input and a physical measure of the input used, in this case, the number of hours worked by stevedores and the number of hours of crane use. The ports included in this study are as follows: Algeciras, Alicante, Bilbao, Cadiz, Cartagena, Castellon, Gijon, Huelva, Corunna, Malaga, Majorca, Alcudia, Motril, Pontevedra, Tenerife, Santander, Seville, Valencia and Vigo. However, as some SEED were created during the study period, the number of observations for each port varies. The above mentioned sources were used to build a data pool with 158 yearly observations for the period from 1990 to 1998.

3.3 Model and Results

As we will consider only the two main inputs, the model to be estimated is the ratio between capital and labour, with the price of the former being used to normalize, such that its demand should be specified. Since the input demand functions are homogeneous of degree zero in ε_i , one of them is unidentified. We normalize ε_K to be unity and estimate ε_L . In order to obtain an explicit expression for the econometric model, let us write the actual demand for capital, X_K^a :

$$X_K^a = \frac{C^a - W_L X_L^a}{W_k} = \frac{C^a}{W_k} - \frac{W_L}{W_k} X_L^a = c^a - w_L X_L^a = \phi(c_{te} - w_L X_{L,te}^a) \quad (26)$$

Now we write the ratio between X_k and X_L , taking into account that this ratio eliminates technical inefficiency keeping allocative inefficiency only. For this we use the normalized version of (5)

$$\frac{X_K^a}{X_L^a} = \frac{c_{te} - w_L X_{L,te}^a}{X_{L,te}^a} = \frac{c_{te}(w^s, Q, t) - (1 + \Omega_L)w_L X_L^a}{X_L^a} \quad (27)$$

Finally, incorporating the parameters that measure the distortion between relative market and shadow prices defined in (3) into (6), the labor demand from (7) and after some manipulation, we get

$$\frac{X_K^a}{X_L^a} = \frac{\alpha_0 + \sum_{r=1}^n \alpha_r Q_r + \frac{1}{2} \sum_{r=1}^n \sum_{l=1}^n \alpha_{rl} Q_r Q_l + \sum_{r=1}^n \alpha_{rt} Q_r t + \alpha_t t + \alpha_{tt} t^2}{\alpha_L + \alpha_{LL} (1 + \Omega_L) w_L + \sum_{r=1}^n \alpha_{Lr} Q_r + \alpha_{Lt} t} \quad (28)$$

Appending a standard error term, equation (28) was estimated using non-linear least squares. Results are shown in Table 1. The estimated input demand function corresponds to a well-behaved production function only if it is monotonically increasing in shadow input prices and output quantities, and concave and linear homogeneous in shadow input prices. Monotonicity is checked by determining if the calculated values of the input demands and cost are positive, which occurs for all observations. Concavity is checked by determining if the principal minors of the Hessian matrix have the correct alternating signs. In this application, the Hessian matrix is a negative semidefinite matrix and therefore concavity in shadow input prices is satisfied. As the NQCF fulfils homogeneity of degree one in prices by construction, the NCQF cost function behind equation (28) presents all the theoretical properties and can be regarded as an adequate representation of the productive structure of cargo handling activities.

We tested three hypothesis related with allocative inefficiency: a) total absence ($\eta_L = \eta_{L_t} = 0$), b) absence of the permanent component ($\eta_L = 0$), and c) absence of temporal variability ($\eta_{L_t} = 0$). Using the Wald test, the first and second hypotheses were rejected at the 1 percent level of significance; the third was rejected at a 5 percent level of significance. With the estimated values of η_L and η_{L_t} we calculated the series for ε_{L_t} using equation (7), which resulted to be less than unity for the whole period. This means that during the 1990-1998 period labour was over utilized regarding capital in cargo handling activities. The average value of ε_L is 0.842, which indicates that the labour-capital mix chosen within this sector was based upon relative prices that were 84.2% of the actual ones. The evolution in time of ε_L shows a continuous decline, which means that the distortion previously described grew within the period, worsening the choice of input combinations.

The estimation of equation (28) yields the parameters that characterize the cost function and the shadow prices. From this, the adjusted optimal labor demand, \hat{X}_L^* , can be calculated using

equation (13). The effects of allocative inefficiency on labor demand, \hat{X}_L^{al} , can be estimated from equation (14) and the cost increase due to this effect, \hat{C}^{al} , can be calculated from equation (19).

Table 1: Results Of Estimation

Parameter	Estimation	T-student
α_L	0.258	11.78
α_{LL}	-26.31	-3.89
α_{MGC}	0.117	6.41
α_{MGNC}	0.429	7.08
α_{GSSI}	0.107	5.63
α_T	-0.006	-4.28
α_{MGCMGC}	0.019	2.16
$\alpha_{MGNCMGNC}$	-0.074	-5.42
$\alpha_{GSSIGSSI}$	0.257	7.02
$\alpha_{MGCMGNC}$	-0.659	-3.89
$\alpha_{MGNCGSSI}$	-0.373	-3.33
$\alpha_{MGCGSSI}$	0.102	2.94
α_{MGCPL}	0.141	8.04
α_{MGNCPL}	0.977	6.84
α_{GSSIPL}	0.110	3.78
α_{TT}	0.002	0.43
α_{TPL}	-0.086	-7.26
α_{TMGC}	-0.002	-0.27
α_{TMGNC}	-0.012	-0.53
α_{TGSSI}	-0.019	-3.25
$\alpha_{CONSTANT}$	0.038	29.47
η_L	-0.029	-2.14
η_{LT}	0.0002	1.54
$R^2 = 0,95$		likelihood ratio test = 171,96

Estimating the optimal amount of the capital and the effect of allocative inefficiency requires a more complex procedure. First, the technically efficient only adjusted input value, $\hat{X}_{K,te}$, can be calculated from the numerator of equation (27). Second, the cost function parameters α_{KL} and α_{KK} can be calculated following the procedure described in the Appendix. Combining these with equation (14), allocative inefficiency, \hat{X}_K^{al} , can be calculated. Finally, optimal input demand can be obtained as the difference, i.e. $\hat{X}_K^* = \hat{X}_{K,te} - \hat{X}_K^{al}$.

From the adjusted values $\hat{X}_{L,te}$ and $\hat{X}_{K,te}$, \hat{X}_L^* and \hat{X}_K^* , we can calculate \hat{C}_{te} and \hat{C}^* whose ratio yields Farrell's allocative efficiency index for each observation, from which time and firm variability can be calculated. Following the procedure described, we estimated the effects of

allocative inefficiency on the demand for labour and capital and on costs, for each observation. The values of the parameters α_{LK} and α_{KK} are 4.09 and -4.72 respectively.

Table 2 shows the average values of allocative inefficiency by port. These results confirm previous intuition regarding a larger than efficient utilization of labour while it would be advisable to use more crane-hours. In average, labour was used 14.4% more than what is efficient; and the use of crane-hours was 13.2% less than optimal.

We have also calculated Farrell's (1957) efficiency indices for each observation. As explained earlier, the allocative index is given by the ratio between the optimum and the technically efficient expenditure, C^*/C_{te} , while the technical index is obtained as the ratio C_{te}/C^a where C^a is the actually observed cost. Both can be calculated for each firm and period. Finally, their product yields Farrell's cost efficiency index. Table 2 shows the average of the three indices for each port.

Table 2: Effects Of Allocative Inefficiency And Farrell's Efficiency Indices

Puerto	Over utilization of labor (%)	Under utilization of capital (%)	Allocative Efficiency Index	Technical Efficiency Index	Cost Efficiency Index
Algeciras	2.6	4.2	0.995	0.965	0.960
Alicante	9.1	16.3	0.893	0.894	0.888
Bilbao	3.8	3.7	0.980	0.922	0.914
Cádiz	12.5	20.6	0.869	0.898	0.796
Cartagena	21.8	18.2	0.929	0.941	0.875
Castellón	15.5	13.4	0.955	0.948	0.919
Gijón	22.1	19.3	0.902	0.928	0.887
Huelva	16.7	16.2	0.933	0.970	0.906
La Coruña	11.9	11.1	0.979	0.924	0.908
Málaga	17.47	17.8	0.846	0.936	0.860
P.Mallorca	19.5	10.9	0.905	0.869	0.859
Alcudia	21.9	19.5	0.931	0.942	0.925
Motril	21.3	11.8	0.880	0.888	0.890
Pontevedra	18.1	19.8	0.944	0.918	0.913
S/C Tenerife	11.2	20.0	0.953	0.821	0.790
Santander	9.5	7.2	0.950	0.757	0.749
Sevilla	20.7	12.4	0.901	0.936	0.901
Valencia	3.8	5.4	0.981	0.948	0.931
Vigo	17.4	16.9	0.945	0.956	0.903
Mean	14.6	13.9	0.931	0.914	0.883

The average of the allocative efficiency index shows that the inadequate choice of labour and capital in Spanish ports meant an extra cost of 6.9%. The largest ports specialized in containers are the most efficient from this viewpoint. On the other hand, technical inefficiency provoked an average extra cost of 8.6%. Finally, average total inefficiency is 11.7%, and the largest container ports of Algeciras and Valencia show the most efficient behavior.

4 CONCLUSIONS

In this paper we have built a theoretical model using a normalized quadratic cost system to decompose, in the line of exact measures, the effects of allocative and technical inefficiency on input demands and cost. For this proposal, we have used the shadow prices approach. Using a panel data allows to obtain individual and time varying inefficiency measures.

The model has been applied to estimate both technical and allocative effects on cost and input demands in handling cargo in Spanish ports during the period of 1990-1998. In average, labour was used 14.6% more than what is efficient; and the use of crane-hours was 13.9% less than optimal. The average of the allocative efficiency index shows that the inadequate choice of labour and capital in Spanish ports meant an extra cost of 6.9%. On the other hand, technical inefficiency provoked an average extra cost of 8.6%. No clear relation with port characteristics can be detected, which very likely indicates differences in management capacity. Finally, average total inefficiency is 11.7%, and the largest container ports show the most efficient behavior.

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REFERENCES

- Atkinson, S. and C. Cornwell (1994a): Parametric Estimation of Technical and Allocative Inefficiency with Panel Data, **International Economic Review** **35**, 231-244.
- Atkinson, S. and C. Cornwell (1994b): Estimation of Output and Input Technical Efficiency using a Flexible Functional Form and Panel Data, **International Economic Review** **35**, 244-255.
- Atkinson, C. and R. Halvorsen (1984): Parametric Efficiency Test, Economies of Scale and Input Demand in U.S. Electric Power Generation, **International Economic Review** **25**, 647-662.
- Atkinson, C. and R. Halvorsen (1990): Tests of Allocative Efficiency in Regulated Multi-Production Firms, **Resources and Energy** **12**, 65-77.
- Bauer, P. W. (1990): Recent Developments in the Econometric Estimation of Frontiers, **Journal of Econometrics** **46**, 39-56.
- Eakin, B.K.(1993): Do Physicians Minimize Cost?, **The Measurement of Productive Efficiency**, H.O. Fried, C.A.K. Lovell y S.S. Schmidt Editores, Oxford University Press.
- Farrell, M.J. (1957): The Measurement of Productive Efficiency, **Journal of the Royal Statistical Society A**, 253-81.
- Greene, W.H. (1980): On the Estimation of a Flexible Frontier Production Model, **Journal of Econometrics** **13**, 101-115.

Kumbhakar, S.C. (1992): Allocative Distortions, Technical Progress and input demand in I.S. Airlines: 1970-1984, **International Economic Review** 33, 723-737.

Kumbhakar, S.C. (1997): Modelling Allocative Inefficiency in a Translog Cost Function and Cost Share Equations: An Exact Relationship, **Journal of Econometrics** 76, 351-356.

Kumbhakar, S.C. and E. Tsionas. (2005): Measuring technical and allocative inefficiency in the translog cost system: a Bayesian approach, **Journal of Econometrics** 126, 355-384.

Maietta. O.W. (2000): The decomposition of cost inefficiency into technical and allocative components with panel data of Italian dairy farms. **European Review of Agricultural Economics** 27, 473-495.

Toda, Y. (1976): Estimation of a Cost Function when Cost Is Not a Minimum: The Case of Soviet Manufacturing Industries, 1958-1971, **Review of Economics and Statistics** 58, 259-268.

APPENDIX: Calculation of α_{KL} and α_{KK} .

Let X_i be factor demand i ($i=1, \dots, m-1$)

$$X_i = X_i(W/W_k, Q, t) \quad (1a)$$

where:

W/W_k is the normalized input price vector

W_k the normalizing price

Q is the product vector

t is trend.

Then:

$$\frac{\partial X_i}{\partial W_k} = \sum_{j \neq k} \frac{\partial X_i}{\partial (W_j/W_k)} \frac{\partial (W_j/W_k)}{\partial W_k} = \sum_{j \neq k} \frac{\partial X_i}{\partial (W_j/W_m)} \left(-\frac{W_j}{W_k^2}\right) = \frac{\partial X_k}{\partial W_i} \quad (2a)$$

Factor demand i from the NQCF is

$$X_i(W/W_k, Q, t) = \alpha_i + \frac{1}{2} \sum_{j \neq k} \alpha_{ij} W_j / W_k + \sum_{r=1}^n \alpha_{ir} Q_r + \alpha_{it} t \quad (3a)$$

Applying (2a) yields:

$$\frac{\partial X_i}{\partial W_k} = -\frac{1}{2W_k} \sum_{j \neq k} \alpha_{ij} W_j / W_k = \frac{\partial X_k}{\partial W_i} \quad (i \neq k) \quad (4a)$$

As factor demands are homogeneous of degree zero in input prices, Euler's theorem yields:

$$\sum_{j=1}^m \frac{\partial X_k}{\partial W_j} W_j = 0 \quad (5a)$$

Solving for $\frac{\partial X_k}{\partial W_k}$ in (5a) and combining with (4a) we get:

$$\frac{\partial X_k}{\partial W_k} = \frac{1}{2W_k^3} \sum_{i \neq k} \sum_{j \neq k} \alpha_{ij} W_i W_j \quad (6a)$$

which permits the calculation of all price effects on input k .